

Manpower Routing and Scheduling with Temporal Dependencies Between Tasks

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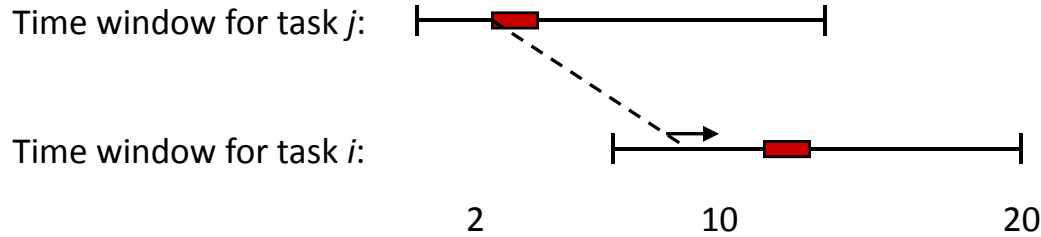
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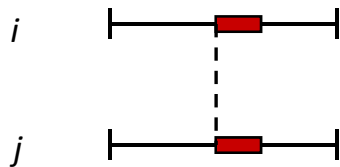
Outline

- What is a temporal dependency?
- Incentive for introducing temporal dependencies.
- Modeling temporal dependencies.
- Branching on time windows.
- Results from practical applications.
- Conclusions.

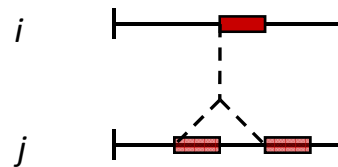
Tasks with Temporal Dependencies



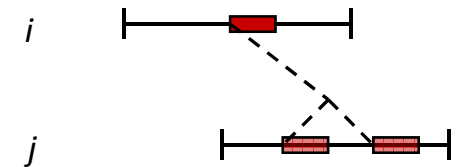
Synchronization:



Overlap:



Min/max gap:



Temporal Dependencies in Practice

- Ground handling in airports
 - Synchronization (Job teaming)
 - Overlap (Not used in practice yet, but is requested by users)
- Home care crew scheduling
 - Synchronization (Mainly for lifting)
 - Overlap (Lifting)
 - Min and max gap (E.g. medication and laundry)
- Allocation of technicians to service jobs [Li et al. 2005].
- Dial-a-Ride for disabled persons [Rousseau et al. 2003].
- Aircraft fleet assignment and routing [Ioachim et al. 1999].
- Machine scheduling with precedence constraints [van den Akker et al. 2006].

The General Temporal Dependency Constraint

$$t_i + p_{ij} \leq t_j$$

Column Generation - Mathematical Model

$$\begin{aligned}
 \min \quad & \sum_{k \in K} \sum_{r \in R^k} c_r^k \lambda_r^k + \sum_{i \in N} c_i \Lambda_i \\
 \text{s.t.} \quad & \sum_{k \in K} \sum_{r \in R^k} a_{ir}^k \lambda_r^k + \Lambda_i = 1 && \forall i \in N \\
 & \sum_{r \in R^k} \lambda_r^k = 1 && \forall k \in K \\
 & \sum_{k \in K} \sum_{r \in R^k} t_{ir}^k \lambda_r^k + p_{ij} \leq \sum_{k \in K} \sum_{r \in R^k} t_{jr}^k \lambda_r^k + M(\Lambda_i + \Lambda_j) && \forall (i, j, p_{ij}) \in P \\
 & \lambda_r^k, \Lambda_i \in \{0, 1\} && \forall k \in K, r \in R^k, i \in N
 \end{aligned}$$

Variables:

$$\lambda_r^k = \begin{cases} 1 & \text{if route } r \text{ is chosen for team } k \\ 0 & \text{otherwise} \end{cases}$$

$$\Lambda_i = \begin{cases} 1 & \text{if task } i \text{ is uncovered} \\ 0 & \text{otherwise} \end{cases}$$

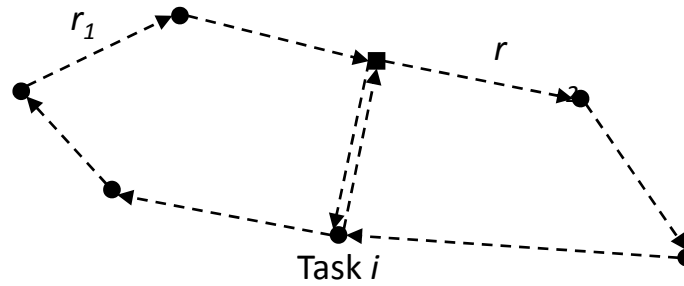
Sets:

N	Tasks
K	Teams / Vehicles
R^k	Routes
P	Temporal Dependencies

Solution Approaches

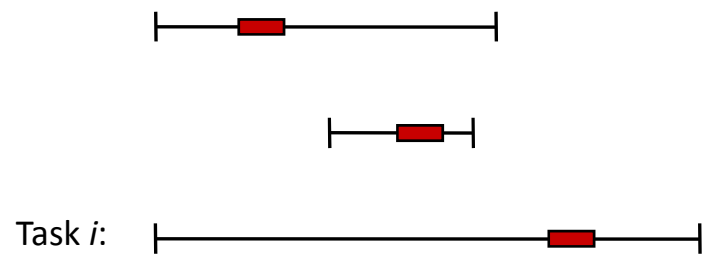
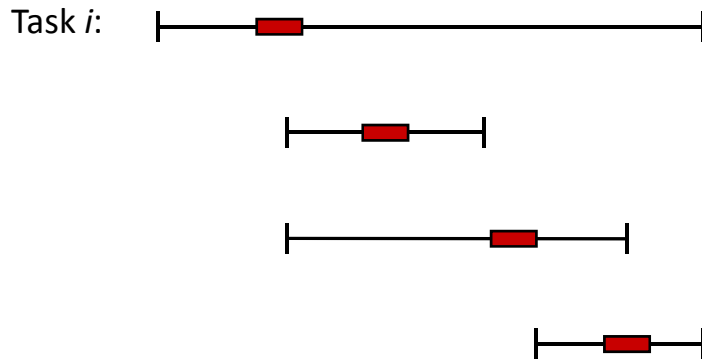
- Relaxing the temporal dependency constraints:
 - The master problem is a Set Partitioning Problem.
 - The subproblem is an Elementary Shortest Path Problem with Time Windows.
 - Temporal dependencies are enforced by branching.
- Solving the presented set partitioning problem with temporal dependency constraints:
 - The master problem is a Set Partitioning Problem with additional non-binary constraints.
 - The subproblem is an Elementary Shortest Path Problem with Time Windows and Linear Node Costs.
 - Only the acyclic case has been considered in the literature [Ioachim et al. 1997].

Visualizing the Routes



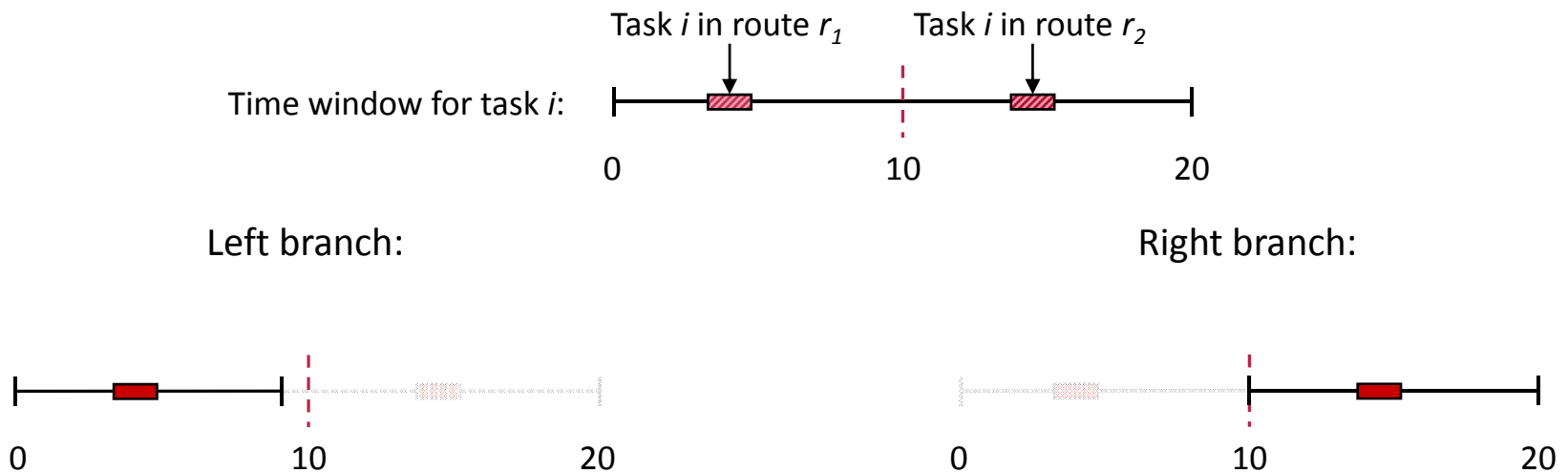
Route r_1 :

Route r_2 :

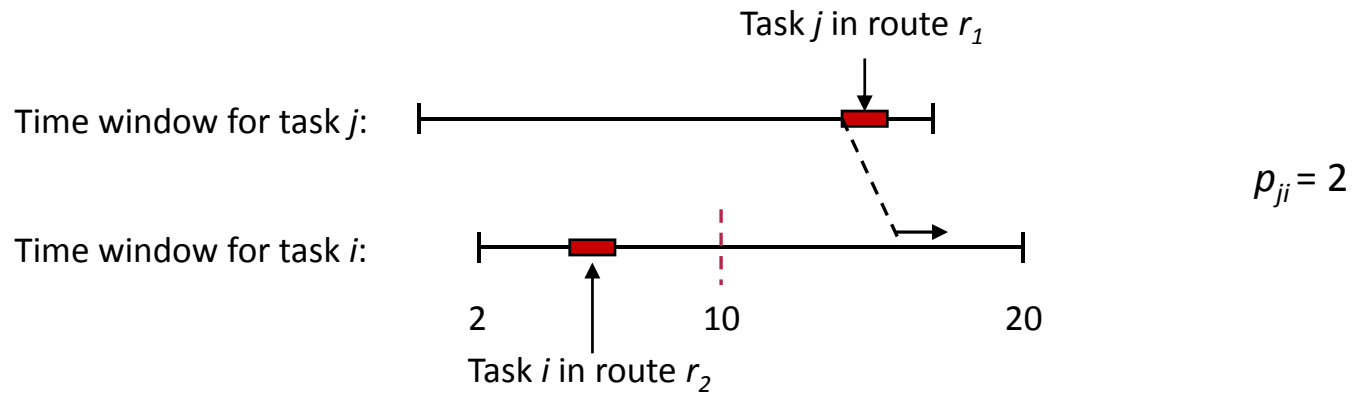


Branching on Time Windows

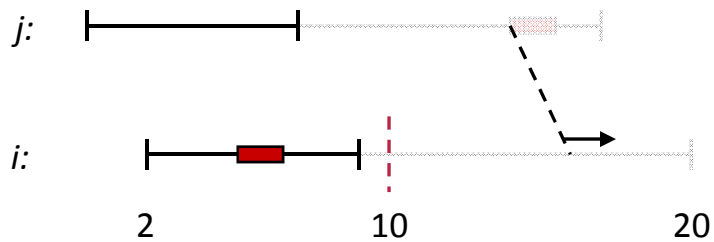
- Will remove most fractional values.
- Will enforce all temporal dependencies.
- Proposed as branching strategy to solely remove fractional values in traditional VRPTW [Gélinas et al. 1995].



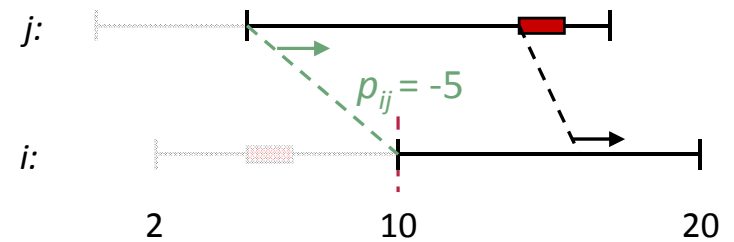
Branching on Time Windows



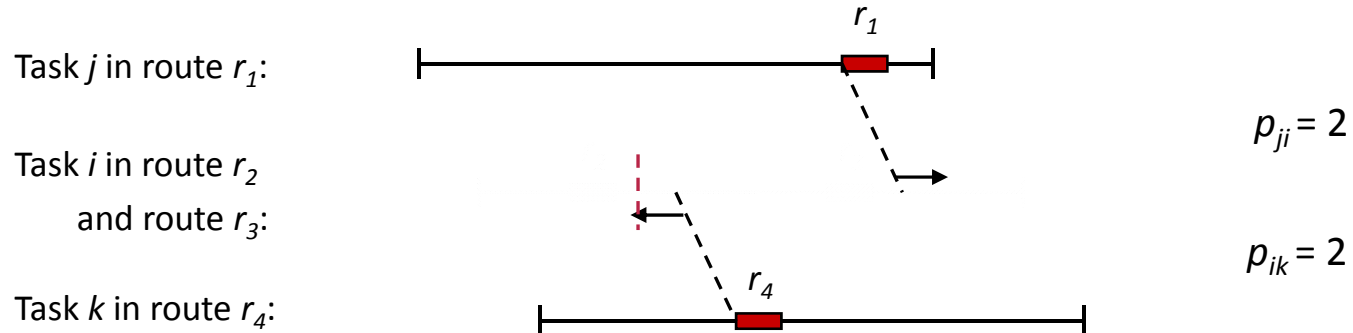
Left branch:



Right branch:



Branching on Time Windows



Infeasible routes:

Left branch:

Right branch:

Branching candidate 1:

r_3, r_1

r_2

Branching candidate 2:

r_3, r_1

r_2, r_4

Branching candidate 3:

r_1

r_2, r_3, r_4

Results - Ground Handling in Airports

- Real-life data from two of Europe's major airports.
- 12 data instances of varying size (12-27 teams, 100-300 tasks):
 - 20-60 synchronization constraints.
 - Optimal solutions for 11 of the 12 datasets.
 - Solutions close to the lower bound for the last dataset.
- Solution time:
 - 6 instances: less than 1 hour.
 - Remaining 6 instances: up to 10 hours.

Results - Home Care Crew Scheduling

- Real-life instances: 6-15 caretakers, 60-150 visits per day.
- Current practice: Tailored heuristic and manual planning
 - Number of uncovered tasks reduced by 50%.
 - In manual planning: Time windows and competence requirements were modified to be able to find feasible solutions.
 - Constraints for up to 20% of tasks were modified in some instances.
 - These adjustments are not allowed in the column generation based optimization.
 - Transportation time is approximately the same as in manual planning.
- Solution time: Less than 1 hour.

Conclusions

- There is a clear incentive for introducing temporal dependencies in the models.
 - Certain combinations are found frequently in practice (e.g. synchronization and overlap)
- The general Temporal Dependency Constraint has been introduced and included in column generation.
 - Various practical problems can be modeled.
- Practical applications show encouraging results.

Thank you for your attention.